Region-specific network plasticity in simulated and living cortical networks: comparison of the center of activity trajectory (CAT) with other statistics

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Abstract

Electrically interfaced cortical networks cultured in vitro can be used as a model for studying the network mechanisms of learning and memory. Lasting changes in functional connectivity have been difficult to detect with extracellular multi-electrode arrays using standard firing rate statistics. We used both simulated and living networks to compare the ability of various statistics to quantify functional plasticity at the network level. Using a simulated integrate-and-fire neural network, we compared five established statistical methods to one of our own design, called center of activity trajectory (CAT). CAT, which depicts dynamics of the location-weighted average of spatiotemporal patterns of action potentials across the physical space of the neuronal circuitry, was the most sensitive statistic for detecting tetanus-induced plasticity in both simulated and living networks. By reducing the dimensionality of multi-unit data while still including spatial information, CAT allows efficient real-time computation of spatiotemporal activity patterns. Thus, CAT will be useful for studies in vivo or in vitro in which the locations of recording sites on multi-electrode probes are important.

Introduction

Modification of connectivity between cortical neurons plays an important role in the processes of learning (Ahissar et al 1992, Buonomano 1998) and memory (Merzenich and Sameshima 1993). Connectivity at the synaptic level has been studied by administering stimuli while simultaneously recording neural activity, and then quantifying plasticity by analyzing the stimulus–response relationships. Culturing on multi-electrode arrays (MEAs) (figures 1(a) and (b)) was introduced to help understand connectivity and plasticity in networks of neurons (Gross 1979, Pine 1980). This allows long-term (months), non-invasive observation of the electrical activity of multiple neurons simultaneously (Potter and DeMarse 2001) in a system with less experimental complexity and greater control than preparations in vivo. External factors such as sensory inputs, attention and behavioral drives are absent, while many aspects of complex spatiotemporal spike patterns observed in animals remain (Gross and Kowalski 1999, Shefi et al 2002).

Many activity statistics have been used to quantify stimulus–response relationships from simultaneous recordings of multiple neurons (Brown et al 2004). Most analyze the dependences between spike trains, such as the maximum likelihood method (Chornoboy et al 1988, Okatan et al 2005), product–moment correlation coefficient (Kudrimoti et al 1999), functional holography (Baruchi and Ben-Jacob 2004), etc. However, only a few were applied for measuring network plasticity. The most common of these was the firing
Population activity statistics

Figure 1. Living MEA culture versus simulated network. The simulated neural network and stimulation electrodes were constructed to mimic the dissociated cultured network and MEA setup. (a) A view of a living MEA culture with 60 electrodes. (b) Neurons, tagged with yellow fluorescent protein, in the highlighted area shown in (a). (c) The structure of a simulated network with 1000 LIF neurons located in a 3 mm by 3 mm region. The circles indicate the neurons, the light-gray lines represent the excitatory synapses and the dark-gray lines represent the inhibitory synapses. All neurons are shown but only 15% of the synaptic connections are shown for clarity. The thick black lines emphasize the connections from a particular randomly selected neuron. (d) The locations of 64 electrodes are shown in circles, and marked with column–row numbers. The connections of the same neuron highlighted in (c) are depicted in light gray.

rate (FR), which showed plastic modifications of network response induced by tetanic stimulation in cortical cultures (Reich et al. 1997, Jimbo et al. 1998, Maeda et al. 1998, Jimbo et al. 1999, Wagenaar et al. 2006a) and dopamine-regulated plasticity in anesthetized rats (Rosenkranz and Grace 1999). Firing rate histogram (FRH) uses firing rates integrated over successive sequential latency epochs to add detailed temporal information, and was applied to demonstrate adaptable image processing and pattern recognition through training by tetanic stimulation in MEA cultures (Ruaro et al. 2005). Mutual information (MI) characterized the statistical dependence between neuron pairs, exposing the strength of coupling between neurons and the functional connectivity among cortical areas (David et al. 2004). Cross-correlation histograms (CCH) from pairs of neurons showed functional plasticity in the auditory cortex of behaving monkeys (Ahissar et al. 1998), and the more advanced shift-predictor corrected cross-correlogram (SCCC) was used to quantify receptive field plasticity in the rat auditory cortex (Bao et al. 2003). Joint peri-stimulus time histogram (JPSTH) characterized the causality of firing between neuron pairs, and successfully demonstrated long-term facilitation of neural activity involved in respiratory control (Morris et al. 2003). Robust neuronal computation and encoding is believed to involve the distribution of information over populations of neurons and synapses in a combination of spatial and temporal domains. Observing only pairs of neurons (MI, CCH, SCCC and JPSTH), neglecting temporal information (FR) and neglecting spatial information (all) limit the ability of these to measure the complex plasticity of the brain.

We recently devised a statistic called the center of activity trajectory (CAT), which incorporates both the physical locations of the recording sites and the timing of neural activity in order to depict dynamics of the population activity in the neuronal circuitry space (Chao et al. 2005). The neuronal circuitry space is defined by the physical locations of the neurons, in our case being the MEA’s two-dimensional plane. The center of activity (CA) component is analogous to the center of mass, in that the ‘mass’ at an electrode location is determined by the recorded
firing rate. CAT is the sequence of CAs over successive time intervals. We discuss how the inclusion of spatial and temporal information improved the detection of neural network plasticity. The importance of the spatial location of neural activity has been widely emphasized in other studies. For example, spatiotemporal dipole models were used to represent the spatial distribution of underlying focal neural sources producing electroencephalographic (EEG) and magnetoencephalographic (MEG) signals (Scherg 1990, Leahy et al 1998).

We used a simulated network to compare CAT’s ability to detect network plasticity to the alternative statistics: FR, FRH, MI, SCCC and JPSTH. No ground truth about network plasticity in living networks exists, because neuronal connectivity cannot be measured for more than a few pairs of neurons simultaneously. Therefore, we could only cross-validate the amount of plasticity detected by each statistic in a simulated network, in which the weights of all synapses were observable. In simulation, we modulated neural plasticity in a controlled manner, and quantified the ability of each statistic to reveal underlying changes in synaptic connectivity.

In simulation, CAT showed the ability to detect smaller changes in the distribution of network synaptic weights than did FR, FRH, MI, SCCC or JPSTH. CAT also detected more pronounced changes in the network following tetanization than the alternate statistics in living MEA cortical cultures.

By applying a shuffling method to the CAT analysis to erase spatial information about recording location in its calculation, we found that changes in activity patterns recorded from neighboring electrodes were not independent and contributed to the better performance of CAT to detect plasticity. The network plasticity was region specific: despite the apparent random connectivity of neurons, plasticity was not symmetrically distributed, and the location of neurons played a role in stimulus-induced plasticity.

**Methods**

**Simulation**

**Simulated networks.** We used the Neural Circuit SIMulator (Natschlager et al 2002) to produce five artificial neural networks, as described previously (Chao et al 2005) (also see supplemental materials 1 available at stacks.iop.org/JNE/4/294). Briefly, 1000 leaky-integrate-and-fire (LIF) model neurons, with a total of 50,000 synapses, were placed randomly in a 3 mm by 3 mm area (see figure 1(c)). All synapses were frequency dependent (Markram et al 1998, Izhikevich et al 2004) to model synaptic depression. 70% of the synapses were excitatory, with spike-timing-dependent plasticity (STDP) (Song et al 2000). We included an 8 by 8 grid of electrodes; 60 of these were used for recording and stimulation as in a real MEA (four excluded electrodes were corner electrodes 11, 18, 81 and 88, see figure 1(d)).

**Setup of networks with different synaptic states.** The synaptic state of a network was determined by its connections and synaptic weight distribution. In order to generate different synaptic states, we used five networks with different connectivity as reference networks. We ran the networks for 5 h in simulated time until the synaptic weights reached a steady state (see supplemental materials 1 available at stacks.iop.org/JNE/4/294). The set of synaptic weights stabilized after 5 h of spontaneous activity, without external stimuli, and was used as the initial state for the corresponding reference network.

For each reference network, we applied simulated tetanization at two randomly picked electrodes at 20 Hz, and a series of subsequent networks (different synaptic states) were collected after different tetanus durations (1, 2, 5, 10, 15, 20, 30 s and 1, 2, 5 min). That is, starting from a reference network \(S_0\), \(S_1\) was the network with the synaptic state at 1 s after the start of tetanization, \(S_2\) at 2 s, and so forth. Therefore, for each pair of randomly chosen tetanization electrodes, ten new networks with different synaptic states were obtained. This process was repeated for each reference state using ten different tetanization electrode pairs. By altering the five reference networks in this manner, a total of 500 new networks with different synaptic states were obtained.

Tetanic stimulation induces long-lasting changes in synaptic transmission (Bliss and Lømo 1973), which shapes how neural circuits process information and is involved in behavioral modifications, including simple forms of learning in motor control (Fisher et al 1997). Administration of 20 Hz tetanization, as in our study, was widely used to induce long-term facilitation (LTF) of post-synaptic potentials at crayfish neuromuscular junctions (Wojtowicz and Atwood 1985, Delaney et al 1989), short-term synaptic plasticity in anesthetized fish (Fortune and Rose 2000), long-term potentiation (LTP) in hippocampal slices (Miles and Wong 1987) and modification of synaptic strength in cortical cultures (Jimbo et al 1999). In our simulated networks, tetanization induced both LTP and long-term depression (LTD) of synapses through STDP: firing of a post-synaptic neuron immediately after a pre-synaptic neuron results in LTP of synaptic transmission and the reverse order of firing results in LTD (Levy and Steward 1983, Markram et al 1998, Bi and Poo 1998, Gerstner et al 1996).

**Simulations with random probing sequence (RPS).** For each network, we ran ten simulations with different 10 min random probing sequences (RPSs). Therefore, a total of 5050 simulations were performed separately on 505 networks (500 new networks and 5 reference networks). The probe stimuli were applied to all 60 electrodes, one at a time, with inter-stimulus intervals on a given electrode drawn from independent exponential distributions with a mean of 60 s. Thus, each electrode stimulated the simulated network with different random sequences, averaging 1 pulse per second for the whole array.

In each simulation, there were 10.0 ± 3.1 (mean and standard deviation) stimuli delivered at each electrode. The same Gaussian noise, introduced into neurons as fluctuations in membrane voltage, was used for each simulation to control the effects of self-firing or of sub-threshold fluctuation of membrane potential on activity. In order to ensure that the
statistics calculated from the same network correspond to the same synaptic state, the STDP algorithm was turned off throughout the simulation to prevent ongoing activity changing the network state.

**Plasticity statistics.** Five commonly used statistics and the center of activity trajectory (CAT) were measured from each simulation (see figure 7). The five commonly used statistics were FR, FRH, mutual information (MI), SCCC and JPSTH (see supplemental materials 2 available at stacks.iop.org/JNE/4/294).

**Center of activity trajectory (CAT).** CAT represents spatiotemporal patterns of network-wide population activity. As applied here, it is a spatially weighted measure of temporally binned responses to single-electrode stimuli in neuronal circuitry space. During each simulation, stimuli at each electrode occurred multiple times (10.0 ± 3.1 times) in one RPS. FRH from the recording electrode $E_k$ to the stimulus at electrode $P_i$, $\text{FRH}_{E_k}^{P_i}$, was defined as the average number of spikes counted in a 5 ms moving time bin with 500 µs time step over trials. $\text{FRH}_{E_k}^{P_i}(n)$ represents the value of $\text{FRH}_{E_k}^{P_i}$ in the $n$th bin, and $\text{Col}(E_k)$ and $\text{Row}(E_k)$ are the column number and the row number of the electrode $E_k$, respectively. For example, the electrode in column number 2 and row number 8 is 28 (see figure 1(d)). The value of CA in the $n$th bin for the stimulation electrode $P_i$ has $X$ and $Y$ components, which are defined as

\[
[C_{X}^{P_i}(n), C_{Y}^{P_i}(n)] = \frac{\sum_{k=1}^{60} \text{FRH}_{E_k}^{P_i}(n)[\text{Col}(E_k) - R_{\text{col}}, \text{Row}(E_k) - R_{\text{row}}]}{\sum_{k=1}^{60} \text{FRH}_{E_k}^{P_i}(n)},
\]

where $R_{\text{col}}$ and $R_{\text{row}}$ are the coordinates of a reference point (the physical center of the 8 by 8 grid of electrodes, in our case). CA was calculated with an electrode number in the neuronal circuitry space, which is equivalent to using the physical location since the inter-electrode spacing is constant. The corresponding $X$ and $Y$ components for CAT are defined as

\[
\text{CAT}_X^{P_i} = [C_{X}^{P_i}(1), C_{X}^{P_i}(2), \ldots, C_{X}^{P_i}(n), \ldots, C_{X}^{P_i}(N)]
\]

\[
\text{CAT}_Y^{P_i} = [C_{Y}^{P_i}(1), C_{Y}^{P_i}(2), \ldots, C_{Y}^{P_i}(n), \ldots, C_{Y}^{P_i}(N)],
\]

where $N$ is the total number of bins in $\text{FRH}_{E_k}^{P_i}$. Intuitively, CA reflects spatial asymmetry of neural activity about the reference point (the center of the dish), and CAT represents the dynamics of CA. That is, if the network is firing symmetrically, the CA will be at the center of the dish, whereas if the network fires mainly in one corner then the CA will be found off-center toward that corner. CA reduces the dimensionality from 60 to 2, and it is not an injective (information-preserving) function of activity distribution. See supplemental materials 3 available at stacks.iop.org/JNE/4/294) for CAT in a simulated network, and Supplemental Materials 5 (available at stacks.iop.org/JNE/4/294) for CAT in an MEA culture.

**Evaluating the performances of different statistics.** Performance of a statistic was defined by the smallest change in network synaptic weights that could be detected as significant. To evaluate performance in each simulation, we evaluated the statistic for evoked responses to all 60 stimulation electrodes and joined these together into a large vector representing the whole stimulus–response information (input–output function) of the network. We called this joint vector the whole-input–output (WIO) vector of the statistic. Figure 2 demonstrates the calculation of the WIO vector for CAT. A visualization of the change in WIO vectors for CAT from $S_0$ to $S_1$–$S_{10}$ appears in figure 3.

We measured the Euclidian distances $E(S_i)$ between ten WIO vectors (from ten simulations with different RPSs) calculated at $S_i$ to the centroidal calculated at $S_0$ (shown as a cross in figure 3). We then compared $E(S_i)$ for $S_1$–$S_{10}$ to $E(S_0)$ separately, and the $p$-values ($n = 10$ RPSs, Wilcoxon signed rank test, which tests the magnitudes of the differences between paired observations without assumptions about the form of the distribution of the measurements) were computed to quantify the significance of differences. For each state, the relation between the mean $p$-values ($n = 50$, from five reference networks and ten tetanization electrode pairs per reference network) and the mean absolute synaptic change (MASC) was quantified

\[
\text{MASC}(S_i) = \frac{1}{N} \sum_{k=1}^{N} \|W_k(S_i) - W_k(S_0)\| \times 100\%,
\]

where $N$ is the number of excitatory synapses and $W_k(S_i)$ represents the synaptic weight of the $k$th excitatory synapse at network $S_i$. We normalized the absolute change in each synapse by the possible range, 0 to 0.5, for excitatory synapses. We determined the performance of different statistics as the minimum MASC for $p$-values below a significance threshold of 0.05; this is termed ‘detectable MASC’. The smaller the MASC a statistic can detect, the better the statistic’s performance.

**Evaluation of the sensitivities and specificities of different statistics.** Successful performance can be artificially enhanced if a statistic mistakes some non-significant changes as being significant. Therefore, analyzing sensitivity (ability to detect significant plasticity) and specificity (ability to discount insignificant plasticity) can further determine the quality of a statistic. Sensitivity was defined as the probability that a statistic indicated a significant difference when calculated from two significantly different network synaptic states (probability of a true positive). Specificity was defined as the probability that a statistic showed no significant difference when calculated from networks with no significant difference in synaptic state (probability of a true negative). Together, sensitivity and specificity described the accuracy of a statistic.

For each reference network, the 500 new states ($S_1$ to $S_{10}$) were individually evaluated to determine whether their synaptic weight distributions were significantly different from the distribution of the reference state (two-sample Kolmogorov–Smirnov test, which tests whether the two samples have the same distribution, two-tailed, $\alpha = 0.05$). If a
Figure 2. Whole-input–output (WIO) vectors for analyzing performances of different statistics. WIO vectors calculated from each statistic were used to represent the network input–output function. As an example, the WIO vector of CAT calculated from probe responses to one RPS at one network state is demonstrated. (a) An RPS, RPS<sub>k</sub>, was delivered into a network with the synaptic state S<sub>i</sub>. (b) CA was calculated for evoked responses to the stimulation electrode P<sub>j</sub> (j = 1 to 60). Each frame indicates the firing rate over a 5 ms moving time window (with a 500 µs time step) on an 8 by 8 grid of electrodes averaged over multiple stimuli at P<sub>j</sub> (RPS<sub>k</sub> might have multiple stimuli delivered at P<sub>j</sub>, see (a)). The 2D trajectory of CAs from frame 1 to frame N (from 0 to 100 ms after the stimuli), CAT, can be represented by a 1D vector by joining CAT<sub>x</sub> and CAT<sub>y</sub>. This vector represents CAT of responses to stimuli P<sub>j</sub> at the network state S<sub>i</sub>. (c) CATs for responses to 60 different stimulation electrodes (P<sub>1</sub> to P<sub>60</sub>) were joined together to form the WIO vector. This WIO vector represents the input–output function, in terms of CAT, of the network state S<sub>i</sub>. For each statistic, each synaptic state has one corresponding WIO vector to describe its input–output function. The statistic that is sensitive to changes in network synaptic states should be able to show significantly different WIO vectors from different synaptic states. One WIO vector was constructed for each RPS (RPS<sub>k</sub>, k = 1 to 10) in each network state (S<sub>i</sub>, i = 0 to 10). Therefore, for each statistic, 5050 WIO vectors were obtained (=500 + 5)×10. 505: 500 new networks + 5 reference networks, 10: number of RPSs delivered to each network).

statistic showed a significant difference (p-value < 0.05; see the previous section) for a state that was significantly different than the reference state (according to the Kolmogorov–Smirnov test), then the result was classified as being a true positive (TP). Conversely, if it showed no significance, then the result was considered a false negative (FN). If a statistic showed significance when calculated from a state that was not significantly different than the reference state, then the result was considered a false positive (FP). If it showed no significance, then the result was considered a true negative (TN). The numbers of TP, FN, FP, and TN were counted for the 500 new networks, and the sensitivity and specificity were defined as

\[
\text{Sensitivity} = \frac{\text{TP}}{\text{TP} + \text{FN}} \times 100\%,
\]

\[
\text{Specificity} = \frac{\text{TN}}{\text{FP} + \text{TN}} \times 100\%.
\]

Experiments in living cultures

Culture and experimental protocol. Dense networks of dissociated cortical neurons were prepared and cultured as described in Potter and DeMarse (2001). Briefly, embryonic rat cortices were dissected and dissociated using papain and trituration. Fifty thousand cells (~7000 cells mm<sup>-2</sup>)
were plated on multi-electrode arrays (MultiChannel Systems, Reutlingen, Germany) pre-coated with poly-ethylene-imine (PEI) and laminin. Cultures were grown in Dulbecco’s Modified Eagle’s Medium (DMEM) containing 10% horse serum. Six experiments were performed on five cultures from four dissociations. Culture ages ranged from 1 to 3 months (Potter and DeMarse 2001). We delivered biphasic stimuli (monopolar) at 500 mV and 400 µs per phase by using our custom-made stimulator (Wagenaar et al. 2004, Wagenaar and Potter 2004). Data acquisition, visualization, artifact suppression (Wagenaar and Potter 2002) and spike detection were performed using MultiChannel Systems hardware and our publicly available acquisition and analysis software, Meabench (Potter et al. 2006). Experiments were conducted in an incubator to control environmental conditions.

Each experiment consisted of a 2 h period of RPS followed by a 15 min tetanic stimulation followed by another 2 h period of RPS (Wagenaar et al. 2006a). In six experiments, the RPS periods consisted of six electrodes stimulated in a random order at an aggregate frequency of 0.5 Hz (in one experiment, the RPS periods consisted of only four probe electrodes). Fewer electrodes were used in RPS for living networks than simulated networks because not every electrode was able to evoke responses. Two of these electrodes were used for the tetanic stimulation: 150 trains of 20 paired pulse stimuli with 10 ms intervals between paired pulses, 50 ms intervals between pairs and 6.5 s intervals between the start of each train. Prior to an experiment, every electrode was stimulated in a random order 20 times, and electrodes with six (or four) highest responses (the total number of spikes counted within 100 ms latency after stimuli over recording electrodes) were selected as probe electrodes. The tetanus electrodes were randomly chosen from these.

Measures of CAT, FR, FRH and SCCC. We used evoked responses within 100 ms after the stimuli of RPS for statistics calculations (see supplemental materials 2 available at stacks.iop.org/JNE/4/294). We measured CAT from the evoked responses in the cultured networks and compared it to the three most commonly used statistics: FR, FRH and SCCC. MI was not measured, due to its poor performance in detecting network plasticity in simulations (see results). JPSTH was not measured because of its high dimensionality and computation time (see figure 7 and supplemental materials 2 available at stacks.iop.org/JNE/4/294).

Statistics. For each statistic, we calculated one WIO vector every 240 s (a ‘block’) for the experiments with six probe stimulation electrodes, and every 160 s for the experiments with four probe stimulation electrodes. Thus, there were 19.9 ± 4.2 (mean and standard deviation) stimuli delivered at each electrode for each WIO vector. Three periods were used for statistics: Pre1, Pre2 and Post1 (see figure 8(a)). Each period had a duration of 52.5 min, and the intervals between Pre1 and Pre2 and between Pre2 and Post1 were 15 min. The 15 min interval between Pre2 and Post1 was the tetanization. For each statistic, the mean distance of the WIO vectors in Pre1 to the centroid of the WIO vectors in Pre2 (C) was compared to the mean distance to their own centroid (D). The ratio of change to drift, C/D, was used to quantify the change from Pre1 to Pre2 before the tetanus (no change if this ratio ≡ 1). A similar measure between Pre2 and Post1 was used to quantify the change across the tetanus. The performance of each statistic to detect the tetanus-induced change was quantified by comparing the two C/Ds (n = 6 experiments, Wilcoxon signed rank test).

Results

We tested the performances of six network plasticity statistics in simulated networks: FR, FRH, MI, SCCC, JPSTH and CAT (all acronyms are shown in table 1).
Figure 4. Comparison of the network activities from a MEA culture and a simulated network. Simulated spontaneous activity and evoked responses resemble the experimentally recorded data. First row: 1 min of spontaneous activity was recorded from a living network by a 60 channel MEA and in simulation for comparison. The upper panels are spike raster plots. The lower panels are firing rate histograms, with bin sizes of 100 ms. Second row: 50 trials of evoked responses recorded by one electrode in a living network and in simulation are shown for comparison. The upper panels are spike raster plots. The lower panels are firing rate histograms with a bin size of 0.1 ms. The timings of stimuli for each trial were aligned at time zero. In the simulation, each electrode recorded the activities occurring within 100 µm.

Table 1. Acronym list.

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Full name</th>
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<tbody>
<tr>
<td>Activity statistics</td>
<td></td>
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<tr>
<td>FR</td>
<td>Firing rate</td>
</tr>
<tr>
<td>FRH</td>
<td>Firing rate histogram</td>
</tr>
<tr>
<td>MI</td>
<td>Mutual information</td>
</tr>
<tr>
<td>SCCC</td>
<td>Shift-predictor corrected cross-correlogram</td>
</tr>
<tr>
<td>CAT/CA</td>
<td>Center of activity trajectory/center of activity</td>
</tr>
<tr>
<td>CAT-ELS</td>
<td>Center of activity trajectory with electrode locations shuffled</td>
</tr>
<tr>
<td>Analyses</td>
<td></td>
</tr>
<tr>
<td>WIO vector</td>
<td>Whole-input–output vector</td>
</tr>
<tr>
<td>CW</td>
<td>Center of weights</td>
</tr>
<tr>
<td>MASC</td>
<td>Mean absolute synaptic change</td>
</tr>
<tr>
<td>C/D</td>
<td>Change-to-drift ratio</td>
</tr>
<tr>
<td>Others</td>
<td></td>
</tr>
<tr>
<td>RPS</td>
<td>Random probing sequence</td>
</tr>
<tr>
<td>MEA</td>
<td>Multi-electrode array</td>
</tr>
<tr>
<td>LIF</td>
<td>Leakly-integrate-and-fire</td>
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<tr>
<td>STDP</td>
<td>Spike-timing-dependent Plasticity</td>
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several of these statistics in their ability to detect tetanus-induced network plasticity in living cultures on MEAs.

Network simulation: CAT showed the highest performance and sensitivity for detecting changes in the network synaptic state

In simulation, the synaptic connectivity can be easily controlled and monitored, and the way(s) changes in synaptic connectivity affect a statistic’s value can be directly studied. Various statistics were used to study functional connectivity in simulated networks under different synaptic states. The performance of different activity statistics to small differences in network synaptic connectivity was evaluated by measuring the statistical significance of the change in each statistic under different network synaptic states, altered gradually by simulated tetanic stimulation with STDP.

Our 1000 neuron LIF model and the living networks expressed similar spontaneous, and evoked, activity patterns, demonstrating the ability of the LIF model to represent the activity of biological networks. Raster plots and FRH of spontaneous activity and evoked responses obtained from both MEA cultures and simulated networks are shown together for comparison, and demonstrate a remarkable similarity of activity patterns (figure 4) (Chao et al 2005). For example, the rates of barrages (the ongoing synchronized bursts of action potentials) were 0.70 Hz and 0.73 Hz, and the proportions of
spikes in barrages were 76% and 71%, in spontaneous activity of living and simulated networks respectively.

A set of simulated networks with different synaptic states was created by using different electrode pairs and durations for tetanizations. In order to verify that different tetanization electrode pairs with different durations changed the synaptic weight distribution in the simulated networks, the centers of weights (CWs) (Chao et al. 2005), see supplemental materials 7 available at stacks.iop.org/JNE/4/294) were used to visualize how the symmetry of the network synaptic weight distribution changed over time. Each curve represents CWs corresponding to a tetanization electrode pair (the column–row numbers of the electrodes are shown at the end of each curve). Synaptic states (S0 to S10) ‘collected’ at different tetanization durations and the corresponding reference state S0 are shown as dots. (b) The relation between mean absolute synaptic change (MASC) and the duration of tetanization (note log scale) from five reference networks. The means and the standard deviations of MASCs are shown (n = 50 networks: from five reference networks, each with ten different tetani).

**Figure 5.** Setup of different synaptic states in simulation. A series of networks with different synaptic states were obtained by tetanization at different electrode pairs and with different durations from the reference network. From each reference network S0, ten tetani at different electrode pairs were delivered. For each tetanization electrode pair, ten synaptic states were obtained after different durations. (a) Different tetanization electrode pairs caused different changes in synaptic weight distribution. The center of weights (CW) (see supplemental materials 7 available at stacks.iop.org/JNE/4/294) was used to visualize how the symmetry of the network synaptic weight distribution changed over time. Each curve represents CWs corresponding to a tetanization electrode pair (the column–row numbers of the electrodes are shown at the end of each curve). Synaptic states (S0 to S10) ‘collected’ at different tetanization durations and the corresponding reference state S0 are shown as dots. (b) The relation between mean absolute synaptic change (MASC) and the duration of tetanization (note log scale) from five reference networks. The means and the standard deviations of MASCs are shown (n = 50 networks: from five reference networks, each with ten different tetani).
network, see results). The mean and standard deviation of the networks with ten different tetanization electrode pairs per reference 50 MASCs were collected from 50 networks (five reference and standard deviation of MASCs (two-tailed, reference states (two-sample Kolmogorov–Smirnov test, two-sample Wilcoxon signed rank test), FRH (p < 0.01) and SCCC (p < 0.01), but not for FR (p = 0.013). C/D was used to quantify the change before the tetanus and the change across the tetanus (if the change is small, C/D ∼= 1). The statistics of C/D from six experiments are shown in figure 8(c).

We did not perform spike sorting for experiments in living cultures. Standard spike sorting methods sort neural signals based on variations in spike waveform. In MEAs, local field potentials and overlapping action potentials distort the waveform to an extreme degree, and the electrodes are too far apart to allow triangulating common signal sources. Spike sorting was attempted, but proved to be unreliable.

**Experiments in living cultures:** CAT revealed tetanus-induced long-term plasticity significantly better than the other statistics

CAT was measured from the evoked responses to RPS in six experiments on living cultured cortical networks (CATs from all experiments are shown in supplemental materials 6 available at stacks.iop.org/JNE/4/294) and compared to the three most commonly used statistics: FR, FRH and SCCC. For visualization purposes, principal components analysis (PCA) was applied to the series of multi-dimensional WIO vectors to capture the largest variances and graphically demonstrate trends in changes. The first two principal components were normalized by subtracting their means and then dividing by their standard deviations. The normalized first principal component (PC1) was plotted versus the normalized second principal component (PC2). An example comparing CAT, FR, FRH and SCCC is shown in figure 8(a). The corresponding CATs before and after tetanization from every block (a 240 s window, see methods) and the average CATs are shown in figure 8(b).

The change across the tetanus was significantly greater than the drift before the tetanus for CAT (p < 1 × 10⁻⁴, Wilcoxon signed rank test), FRH (p < 0.01) and SCCC (p < 0.01), but not for FR (p = 0.013). C/D was used to quantify the change before the tetanus and the change across the tetanus (if the change is small, C/D ∼= 1). The statistics of C/D from six experiments are shown in figure 8(c).

We did not perform spike sorting for experiments in living cultures. Standard spike sorting methods sort neural signals based on variations in spike waveform. In MEAs, local field potentials and overlapping action potentials distort the waveform to an extreme degree, and the electrodes are too far apart to allow triangulating common signal sources. Spike sorting was attempted, but proved to be unreliable.

**Electrode shuffling demonstrates the importance of electrode locations shown by CAT**

In order to get some idea of the degree of localization of function in cultured cortical networks, the performance of CAT statistic with electrode locations shuffled (CAT-ELS) was calculated (see supplemental materials 2 available at stacks.iop.org/JNE/4/294). In CAT-ELSs, the information about the physical locations of the recording electrodes was removed. In both simulations and experiments in living cultures, the electrode locations were shuffled ten times, and ten different corresponding CAT-ELSs were generated. The
Figure 7. Comparison of the six different statistics. CAT was the most sensitive activity statistic and was highly efficient. Examples of six statistics calculated from the same RPS during three synaptic states are shown: \( S_0 \) (reference network), \( S_7 \) (network with \( \sim 50\% \) of the maximal MASC, see figure 5(b)) and \( S_{10} \) (network with the maximal MASC). All statistics were obtained from the same randomly chosen stimulation electrode. CAT: CATs are plotted as CAT\(_x\) versus CAT\(_y\) from blue to red. FR: number of spikes per ms at each recording electrode is displayed according to the corresponding location in the 8 by 8 grids. FRH: FRHs, in the unit of number of spikes per ms, from a randomly chosen recording electrode are plotted. MI: MIs above 0.75 bits are plotted as colored lines between the corresponding electrode pairs. SCCC: SCCCs above zero from a randomly chosen pair of recording electrodes are plotted. JPSTH: JPSTH from the same randomly chosen pair of recording electrodes are shown. The performance (quantified by detectable MASC), compute time and dimensionality, normalized by the values for CAT, are shown on the right. The axes for detectable MASC, compute time and dimensionality are shown on the bottom in red, green and blue respectively (the latter two are with logarithmic scales). Among all six statistics, only FR and FRH had shorter compute time than CAT, and only FR had smaller dimensionality than CAT. However, CAT had significantly smaller detectable MASC than FR and FRH. CAT showed significantly higher performance to detect the difference in the network synaptic state than other statistics.

Table 2. Sensitivity versus specificity in simulated networks.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>CAT</th>
<th>JPSTH</th>
<th>SCCC</th>
<th>FRH</th>
<th>MI</th>
<th>FR</th>
<th>CAT-ELS (ten shuffles)</th>
</tr>
</thead>
<tbody>
<tr>
<td>True positive (%)</td>
<td>77.6</td>
<td>70.4</td>
<td>68.0</td>
<td>47.4</td>
<td>44.0</td>
<td>27.2</td>
<td>30.6</td>
</tr>
<tr>
<td>False negative (%)</td>
<td>8.8</td>
<td>16.0</td>
<td>18.4</td>
<td>39.0</td>
<td>42.4</td>
<td>59.2</td>
<td>55.8</td>
</tr>
<tr>
<td>True negative (%)</td>
<td>11.2</td>
<td>11.0</td>
<td>11.2</td>
<td>12.2</td>
<td>13.6</td>
<td>13.6</td>
<td>12.6</td>
</tr>
<tr>
<td>False positive (%)</td>
<td>2.4</td>
<td>2.6</td>
<td>2.4</td>
<td>1.4</td>
<td>0</td>
<td>0</td>
<td>1.0</td>
</tr>
<tr>
<td>Sensitivity (%)</td>
<td>88.7</td>
<td>83.8</td>
<td>78.7</td>
<td>54.9</td>
<td>50.9</td>
<td>31.5</td>
<td>35.4</td>
</tr>
<tr>
<td>Specificity (%)</td>
<td>82.4</td>
<td>81.2</td>
<td>82.4</td>
<td>90.6</td>
<td>100</td>
<td>100</td>
<td>92.9</td>
</tr>
</tbody>
</table>

performance of these CAT-ELSs was evaluated and compared to the original CAT.

CAT, unlike the other statistics, incorporates the physical locations of the recording electrodes. This is the primary difference between methods, and we attribute CAT’s superior performance in both living and simulated networks to this feature. For simulated networks, the comparison of the performance between CAT-ELS and original CAT is shown in figure 9(a). The detectable MASC (threshold \( p \)-value = 0.05) for mean CAT-ELS was 10.8\%, which was worse than CAT
(a) An example of comparison of CAT, FR, FRH and SCCC (from evoked responses to RPS in one experiment) before and after tetanization is shown. Principal components analysis (PCA) was applied on multi-dimensional WIO vectors for visualization purposes. The normalized principal component was obtained by removing its mean and then dividing through by its standard deviation. The normalized first principal component (PC1) was plotted versus the normalized second principal component (PC2). Each dot represents the statistic calculated from every block (a 240 s window), and the color indicates the corresponding time (shown in the colorbar). The black dashed line represents the tetanus. The separation between pre-tetanization clusters (bluish dots) and post-tetanization clusters (reddish dots) indicates the change of the statistic across the tetanus. (b) Different patterns of CATs were observed before and after tetanization. CATs from an example experiment were overlaid (black trajectories), and the average CATs were shown by series of circles (from blue to red across 100 ms probe response). The trajectories for every experiment can be found in the supplemental materials 6 (available at stacks.iop.org/JNE/4/294). (c) The statistics of $C/D$ from six experiments showed that the change across the tetanus was significantly greater than the drift before the tetanus for CAT (**, $p < 1 \times 10^{-4}$, Wilcoxon signed rank test), FRH (*, $p < 0.01$) and SCCC (*, $p < 0.01$), but not for FR ($p = 0.013$). The $p$-values indicate that CAT was more capable of detecting the change over the drift than FRH, SCCC and FR.

(4.68%). The decrease in performance (increase in detectable MASC) indicates that electrode locations significantly affect the performance of CAT in simulated networks. Furthermore, the sensitivity of CAT-ELS was 35.4%, significantly smaller than CAT’s 88.7% (see table 2).

For living MEA cultures, one example of the comparison between CAT and CAT-ELS is shown in figure 9(b). The corresponding CAT-ELSs before and after tetanization from every block are shown in figure 9(c). The electrode location shuffling ‘collapsed’ the patterns of CAT-ELSs before and after tetanization (compare to figure 8(b)). The difference between pre-tetanization and post-tetanization clusters found in CAT was also reduced in CAT-ELS (figure 9(b)).

The statistics of $C/D$ for CAT-ELS ($n = 60$, six experiments, ten shuffles for each experiment) are shown in figure 9(d). The change across the tetanus was significantly greater than the drift before the tetanus for CAT ($p < 1 \times 10^{-4}$, Wilcoxon signed rank test), but not for CAT-ELS ($p = 0.19$).

**Discussion**

Statistics of functional plasticity in extracellular multi-electrode recordings

While comparisons of firing rates show plasticity in intracellular recordings, more detailed statistics incorporating spatiotemporal population activity patterns are needed to reveal plasticity in extracellular multi-electrode recordings. Electrode spacing on the order of hundreds of microns means that any induced or observed plasticity will span pathways of multiple neurons instead of neighboring monosynaptic neurons (Jimbo *et al* 1999). Intracellularly, synaptic strength
is directly observable by stimulating a pre-synaptic neuron while recording from an adjacent post-synaptic neuron. Extracellulary, synaptic noise across a chain of neurons and convergent pathways will obscure firing rate measures of stimulus-induced plasticity.

Alternatively, by incorporating the timing and spatial flow of activity, spatiotemporal patterns have been found both in vivo and in vitro. Spike sequences, imposed upon the network by behavioral manipulations, recur spontaneously during subsequent sleep episodes (Nádasdy et al. 1999, Nádasdy 2000, Lee and Wilson 2002). Calcium imaging of cortical slices reveals reactivation of sequences of neurons, ‘cortical songs’, with distinct spatiotemporal structures over tens of seconds (Ikegaya et al. 2004). Robust recurrent spike patterns were also found in a detailed cortical simulation (Izhikevich et al. 2004) and in living slices (Fellous et al. 2004). CAT provides a new and simple statistic to detect spatiotemporal patterns in networks and extends the previous studies by quantifiably demonstrating its ability to discern plasticity.

**Region-specific plasticity**

Although FRH included detailed temporal information about the activity dynamics at all electrodes, it was less capable of capturing network plasticity than CAT, which has the same temporal resolution as the FRH but ‘condenses’ the spatial dimension by linear combination (see equation (1)). We hypothesize that this was due to the inclusion of spatial information of the electrode locations. The performance and the sensitivity of CAT with electrode locations shuffled were significantly worse than unshuffled CAT, both in simulation (the detectable MASC increased from 4.68% to 10.8% and the sensitivity decreased from 88.7% to 35.4%) and in living networks (the change across the tetanus was significantly greater than the drift before the tetanus for CAT, but not for CAT-ELS) (see figure 9 and table 2). This indicates that activity varied systematically with the electrode location, and also suggested that the observed network plasticity was region specific: the plasticity was not symmetrically distributed throughout the network. This further suggests that despite
the apparent random connectivity of cultured neurons, neuron location played a role in tetanus-induced plasticity.

Region specificity was not limited to plasticity induced by tetanization. In simulation, we also altered the weights of randomly selected synapses in reference networks to different degrees to generate different new network states. CAT still showed the highest sensitivity to changes in MASC, and furthermore, the sensitivity of CAT-ELS was still significantly lower (data not shown). Despite the synaptic plasticity not being region specific, the spatiotemporal flow of neural activity was region dependent, effectively making the plasticity of neural activity region specific. This result supports the notion of synfire chains or braids of neural activity (Ikegaya et al. 2004, Izhikevich 2005), where information is transmitted in a pipeline of neighboring pathways as opposed to a single string of connections. In this study, tetanization was used to obtain different synaptic states since it provided a realistic form of plasticity and a straightforward comparison to our study of local functional plasticity in living networks.

A common misconception regarding dissociated cultures is that they are random, homogeneous and lack structure, and thus cannot support stable changes to synaptic weights associated with memory formation. While plated from a random cell suspension, microscopic observation reveals that a heterogeneous arrangement develops over time (Gross and Kowalski 1999, Segev et al. 2003). Although very different than structures found in vivo, the ability of neurons and glia to interact remains and a network having a diverse array of activity arises spontaneously (Wagenaar et al. 2006b). Altering sensory input of thalamic relays to cortical areas has demonstrated that the cortex develops structure according to the type of the sensory input (Sur et al. 1988), which suggests an important relationship between neural structure and function. CAT demonstrates that structure is also relevant to neural function in a cultured network, and that tetanic stimulation alters network function. Future experiments will incorporate closed-loop sensory-motor feedback and optical imaging to investigate the network mechanisms of our cultures to functionally and structurally adapt to environmental interaction (Potter et al. 2006).

CAT versus population coding

It is important to note that CAT is distinct from the population vector description of neural activity (Georgopoulos et al. 1986, Caminiti et al. 1990). Population coding, which is widespread in the brain and in invertebrate nervous systems, has been found in the motor cortex (Georgopoulos 1994), premotor cortex (Caminiti et al. 1990), hippocampus (Wilson and McNaughton 1993) and other cortical areas. It demonstrates how the firing rates of a group of broadly tuned (e.g., to a direction of arm movement) neurons, taken together, provide an accurately tuned representation. With population codes, a fixed-weight linear combination of neuronal activity is projected in a sensory input space or a motor output space (Carmena et al. 2003). In contrast, CAT incorporates information about the physical recording locations into its linear combination calculation, and projects neuronal activities recorded at different sites into the actual neuronal location space in order to depict the dynamics of the population activity. Furthermore, the linear combination of activities in CAT is normalized by the total firing rate across all electrodes (see equation (1)).

CA is a measure of the asymmetry of the spatial activity distribution, and CAT is a measure of its dynamics. A similar measure of population activity flow was applied in human study to quantify the trajectory patterns of the traveling electroencephalographic alpha waves across the scalp (Manjarrez et al. 2007).

Plasticity versus spontaneous bursting

Without external stimulation, the most prominent feature of spontaneous activity found in MEA cultures and in simulated networks is synchronous bursting (Wong et al. 1993, Kamioka et al. 1996, Gross and Kowalski 1999, Van Pelt et al. 2004, Wagenaar et al. 2005), and bursts were found to have effects on tetanus-induced synaptic plasticity in cortical neurons (Maeda et al. 1998). In simulation, the network synaptic state after tetanization was found to change gradually due to the presence of spontaneous bursts, which makes quantifying tetanus-induced plasticity difficult (Chao et al. 2005). In the six experiments we performed on living MEA cultures, 8.57 ± 3.33 spontaneous bursts per minute and 16.06 ± 4.55 stimulus-evoked bursts per minute were observed. Even with the presence of the spontaneous bursts, the tetanus-induced plasticity was still detected by using CAT. Since the level of bursting can be finely controlled in MEA cultures with multisite stimulation (Wagenaar et al. 2005), we plan to use CAT to investigate how the degree of bursting affects a network’s ability to produce and/or maintain plasticity.

CAT’s superior performance, sensitivity and low computational load make it an attractive method for real-time applications. CAT can also be applied to in vivo multi-electrode or optical recording studies for neural activity aligned to behavioral or sensory cues. As techniques for observing distributed activity become faster and more fine-grained, studying the details of the spatial flow of activity through neuronal networks will reveal more and more about processes of learning and memory.

Acknowledgments

This work was partially supported by grants NS38628 from NIH/ENV/DS, EB000786 from NIH/NIBIB and DA18250 from NIH/NIDA, and by the Whitaker Foundation and the NSF Center for Behavioral Neuroscience. We thank Radhika Madhavan for technical assistance and Douglas Swehla for valuable inputs.

References


Baruchi I and Ben-Jacob E 2004 Functional holography of recorded neuronal networks activity J. Neuroinform. 2 333–52

Bi G Q and Poo M M 1998 Synaptic modifications in cultured hippocampal neurons: dependence on spike timing, synaptic strength, and postsynaptic cell type J. Neurosci. 18 10464–72

Bliss T V and Lomto T 1973 Long-lasting potentiation of synaptic transmission in the dentate area of the anaesthetized rabbit following stimulation of the perforant path J. Physiol. 232 331–56


Izhikevich E M 2005 Polychronization: computation with spikes Neural Comput. 18 245–82


Lee A and Wilson M 2002 Memory of sequential experience in the hippocampus during slow wave sleep Neuro 36 1183–94

Levy W B and Steward O 1983 Temporal contiguity requirements for long-term associative potentiation/depression in the hippocampus Neuroscience 8 791–7


Manjarrez E, Vazquez M and Flores A 2007 Computing the center of mass for traveling alpha waves in the human brain Brain Res. 1145 239–47


Miles R and Wong R K 1987 Inhibitory control of local excitatory circuits in the guinea-pig hippocampus J. Physiol. 385 611–29


Nádasdy Z 2000 Spike sequences and their consequences J. Physiol. 94 505–24


Population activity statistics


Rosenkranz J A and Grace A A 1999 Modulation of basolateral amygdala neuronal firing and afferent drive by dopamine receptor activation in vivo J. Neurosci. 19 11027


Scherg M 1990 Fundamentals of dipole source potential analysis Adv. Audiol. 6 40–69


Wagenaar D, Pine J and Potter S M 2006a Searching for plasticity in dissociated cortical cultures on multi-electrode arrays J. Negat. Results Biomed. 5 16

Wagenaar D A, Pine J and Potter S M 2006b An extremely rich repertoire of bursting patterns during the development of cortical cultures BMC Neurosci. 7 11


Wagenaar D A and Potter S M 2004 A versatile all-channel stimulator for electrode arrays, with real-time control J. Neural Eng. 1 39–44

Wilson M and McNaughton B 1993 Dynamics of the hippocampal ensemble code for space Science 261 1055–8

Wojtowicz J M and Atwood H L 1985 Correlation of presynaptic and postsynaptic events during establishment of long-term facilitation at crayfish neuromuscular junction J. Neurophysiol. 54 220–30

Wong R O L, Meister M and Shatz C J 1993 Transient period of correlated bursting activity during development of the mammalian retina Neuron 11 923–38

308
Supplement for:

Region-specific Network Plasticity in Simulated and Living Cortical Networks: Comparison of the Center of Activity Trajectory (CAT) With Other Statistics

Zenas C. Chao, Douglas J. Bakkum and Steve M. Potter

S1: Simulated networks.

Features:

The Neural Circuit SIMulator (Natschlager et al., 2002) was used to produce five artificial neural networks as described previously (Chao et al., 2005). Briefly, 1,000 leaky-integrate-and-fire (LIF) model neurons with a total of 50,000 synapses were placed randomly in a 3mm by 3mm area (see figure 1(c)). All synapses were frequency-dependent (Markram et al., 1998; Izhikevich et al., 2004) to model synaptic depression. 70% of the neurons were excitatory, with spike-timing dependent plasticity (STDP) (Song et al., 2000). The other neurons were inhibitory (30%) (Marom and Shahaf, 2002). Neurons made many short synaptic connections but a few long ones as well (Segev and Ben-Jacob, 2000). The number of synaptic connections per neuron followed a Gaussian distribution and each neuron had 50 ± 33 synapses onto other neurons (no multiple synapses from one neuron to another).

The conduction delay was proportional to the distance between somata, and the conduction velocity was set to be 0.3 m/s (Kawaguchi and Fukunishi, 1998). Gaussian random noise was introduced into each neuron independently as fluctuations in membrane voltage: 30% of the neurons (“self-firing neurons”) had variance at a high enough level to initiate spikes (Latham et al., 2000), while the
rest exhibited only subthreshold fluctuations. An 8 by 8 grid of electrodes was
included, 60 of these (except corner electrodes 11, 18, 81 and 88) were used for
recording and stimulation as in a real MEA (figure 1(d)). A stimulation electrode
stimulated 76 ± 12 (n= 5 simulated networks) of the closest model neurons.

**Setup of network initial states:**

All excitatory synaptic weights were initially set to 0.25 and could vary between
zero and 0.5 due to STDP. At the maximal weight, each spike would have a 90%
probability of evoking a spike in the post-synaptic neuron, due to its summation
with intrinsic noise. The synaptic weights for the inhibitory connections were fixed
at -0.25. The networks were run for 5 hours in simulated time until the synaptic
weights reached a steady state. Most of the excitatory synaptic weights (92 ± 3%)
in the 5 reference networks were less than 0.05 or greater than 0.45. This bimodal
steady-state distribution of weights arose from the STDP rule, as previously
observed by Song et al. (Song et al., 2000), and Izhikevich and Desai (Izhikevich
and Desai, 2003). The set of synaptic weights after 5 hours of spontaneous activity
stabilized, without external stimuli, and was used as the initial state for the
corresponding reference network.
S2: Calculations of the statistics for experiments in simulations and living cultures.

The evoked responses within 100 msec (to include all evoked responses) after the stimuli of random probing sequences (RPSs) were used for calculations of the statistics. The dimensionalities of different statistics are shown in Table S1. For those statistics include temporal information (FRH, MI, SCCC, JPSTH, and CAT), responses within 100 msec were binned by a 5 msec moving time bin with 500 µsec time step. 500 µsec time step was used to obtain fine temporal resolution, since it was less than the occurrence of an action potential. 5 msec bin size was used to acquire action potentials on multiple electrodes within a single bin. Also, the same binning parameters were used for all statistics in simulations and in living cultures for fair comparison of their performance.

1. Simulations:

Firing Rate (FR)

This most commonly used statistic quantifies the intensity of the evoked responses. During each simulation, stimuli at each electrode occurred multiple times (10.0 ± 3.1 trials) in one RPS. FR for evoked responses to each stimulation electrode was calculated by averaging the number of spikes counted at each recording electrode over trials, producing a 60-dimensional vector.

Firing Rate Histogram (FRH)

FRH expands on FR by including temporal information. FRH from recording electrode $E_k$ to the probing stimulus at electrode $P_i$, $FRH^E_{P_i,k}$, was the average number of spikes counted in a 5 msec moving time window with 500 µsec time
step over trials, which resulted in a 1X191 vector. FRH for evoked responses to
stimulation electrode $P_i$ was defined by joining $FRH^i_{E_k}$ from 60 recording
electrodes together, which formed an 11,460-dimensional (191X60) vector.

**Center of Activity Trajectory (CAT)**

The definition of CAT is described in Methods (Equation 1 and 2). The X and Y
components are both 1X191 vectors. By appending two components together,
CAT for evoked responses to each stimulation electrode was a 382-dimensional
(191X2) vector.

**Mutual Information (MI)**

MI quantifies the statistical dependence, including higher order moments in
addition to 2nd order, between responses at different locations (Moddemeijer,
1989; Brunel and Nadal, 1998; Paninski, 2003). MI between two recording
electrodes $E_k$ and $E_j$ for stimulation electrode $P_i$ is defined as the mutual
information between two distributions: $FRH^i_{E_k}$ and $FRH^i_{E_j}$. Let $FRH^i_{E_k} =$

$$\{A_n\}_{n=1}^{191}$$ and $FRH^i_{E_j} = \{B_m\}_{m=1}^{191}$, where $A_n$ and $B_m$ represent elements in FRHs.

Then the MI between $FRH^i_{E_k}$ and $FRH^i_{E_j}$ is defined as:

$$I(FRH^i_{E_k} , FRH^i_{E_j}) = \sum_{n,m} P_{X,Y}(A_n \times B_m) \ln \frac{P_{X,Y}(A_n \times B_m)}{P_X(A_n) \times P_Y(B_m)}$$

where $P_X$ and $P_Y$ represent the marginal probabilities of $FRH^i_{E_k}$ and $FRH^i_{E_j}$, and

$P_{X,Y}$ represents the joint probability of $FRH^i_{E_k}$ and $FRH^i_{E_j}$. MI was estimated by
using the histogram-based mutual information methods described by

Moddemeijer (Moddemeijer, 1989). In this study, the MATLAB codes from
Rudy Moddemeijer’s group were used. MI provides a non-directional connectivity map, which represents the dependence between activities at different pairs of electrodes. By joining the MI from every pair of electrodes, MI for evoked responses to each stimulation electrode was a 1,770-dimensional (60X59/2) vector.

**Shift-predictor Corrected Cross-Correlogram (SCCC)**

The corrected cross-correlogram (Michalski et al., 1983; Eggermont, 1992; Brody, 1999; Franco et al., 2004; Ventura et al., 2005) removes the peak in the original cross-correlogram that is due to co-stimulation of the neurons, and measures the association between neurons. For each pair of recording electrodes, the “raw” cross-correlogram was constructed by averaging the cross-correlograms between two spike trains from the two electrodes over trials. The “shift predictor” was constructed by averaging the cross-correlograms between all possible pairs of spike trains from the two electrodes but from different trials. SCCC was then the raw cross-correlogram minus the shift predictor. In this study, the algorithm described by George Gerstein’s group was used.

With the same binning resolution used for FRH, SCCC between each pair of recording electrodes was a (191X2-1)-dimensional vector which represents the correlations sequence at different lags. Therefore, SCCC for evoked responses to each stimulation electrode was a 674,370-dimensional ((191X2-1)X60X59/2) vector.

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2. [http://mulab.physiol.upenn.edu/crosscorrelation.html](http://mulab.physiol.upenn.edu/crosscorrelation.html)
Joint Peri-Stimulus Time Histogram (JPSTH)

The JPSTH quantifies the causality between responses at different locations (Gerstein and Perkel, 1969; Aertsen et al., 1989; Ventura et al., 2005). JPSTH finds the fixed delay between sequences of spikes recorded at different pairs of neurons (electrodes) over multiple trials, which can depict causal relationships between them. Similar to SCCC, the shift-predictor was applied on the “raw” JPSTH to eliminate the time-locked stimulus-induced covariation due to co-stimulation. In this study, the algorithm and MATLAB codes from George Gerstein’s group were used\(^3\). The results can provide directional information about the connectivity. With the same binning resolution used for FRH, JPSTH between each pair of recording electrodes was 191X191-dimensional. Therefore, JPSTH for evoked responses to each stimulation electrode was a 64,571,370-dimensional (191X191X60X59/2) vector.

Center of Activity Trajectory with Electrode Locations Shuffled (CAT-ELS)

The electrode locations, \(E_k\), were randomly shuffled. Then CAT-ELS was calculated according to Equation 1 and 2 (in Methods) by using these shuffled electrode locations. For each network, the electrode locations were shuffled 10 times and 10 different corresponding CAT-ELSs were generated.

2. Experiments in living cultures:

Firing Rate (FR)

The number of spikes was counted at each recording electrode for each probe response and averaged every block. Thus, for each stimulation electrode, a

\(^3\) [http://mulab.physiol.upenn.edu/jpst.html](http://mulab.physiol.upenn.edu/jpst.html)
60-dimensional FR vector was obtained for every 240 sec (“block”, see Methods).

Firing Rate Histogram (FRH)

For evoked responses to each stimulus, the FRH was calculated by using a 5 msec moving time window with time step of 500 μsec. Thus, for each stimulation electrode, an 11,460-dimensional (191X60) FRH vector was obtained for every block.

Center of Activity Trajectory (CAT)

Let $FRH_{E_i}^{P_i}$ be the average responses over each block, recorded at electrode $E_i$ to stimulation electrode $P_i$, CAT for stimulation electrode $P_i$ was then calculated from the $FRH_{E_i}^{P_i}$ by using Equation 1 and 2 (in Methods). Thus, for each stimulation electrode, a 382-dimensional (191X2) CAT vector was obtained for every block.

Shift-predictor Corrected Cross-Correlogram (SCCC)

With the same binning resolution used for FRH, SCCC between each pair of recording electrodes was calculated for every block. Thus, for each stimulation electrode, a 674,370-dimensional ((191X2-1)X60X59/2) SCCC vector was obtained for every block.

Center of Activity Trajectory with Electrode Locations Shuffled (CAT-ELS)

CAT-ELS was calculated by the same shuffling procedure used in simulations. For each experiment, the electrode locations were shuffled 10 times and 10
different corresponding CAT-ELSs were generated. The dimensionality of
CAT-ELS was the same as CAT.

Table S1. The dimensionality of the statistics.

<table>
<thead>
<tr>
<th>Statistics</th>
<th>Dimensionality(^1)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Simulations</td>
</tr>
<tr>
<td>FR</td>
<td>60</td>
</tr>
<tr>
<td>FRH</td>
<td>11,460</td>
</tr>
<tr>
<td>MI</td>
<td>1,770</td>
</tr>
<tr>
<td>CAT</td>
<td>382</td>
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<tr>
<td>CAT_ELS</td>
<td>382</td>
</tr>
<tr>
<td>SCCC</td>
<td>674,370</td>
</tr>
<tr>
<td>JPSTH</td>
<td>64,571,370</td>
</tr>
</tbody>
</table>

\(^1\) The dimensionality is defined as the length of the statistic calculated from evoked
responses to one stimulation electrode in one simulation or in one block (for
experiments in living cultures).
S3: Movie of CATs in a simulated network.

Different patterns of CATs were obtained from evoked responses to stimuli at different electrodes in simulation (see Movie S3). **A.** The rasterplot of 1 second of network activity from 1000 LIF neurons. Evoked responses to stimuli at different electrodes are shown in different colors. **B.** 1000 neurons on 3mm by 3mm area. Neurons are shown as gray dots, and the active synapses are shown in cyan lines. The locations of stimulation electrodes are indicated by crosses with the corresponding colors shown in A. **C.** The corresponding CATs. The color of the trajectory represents the corresponding evoked response shown in A. Time is represented in the red bar at the bottom of A.

Sorting recorded action potentials and recalculating the activity statistics improved the performance of all except for CAT. However, the CAT still showed the highest performance. The calculation of the CAT remained the same as the sorted spikes are spatially summed according to recording electrode locations. The six statistics were re-calculated based on the activity of about 250 spike sorted neurons instead of 60 electrodes (see Results). JPSTH, SCCC, FRH, MI and FR improved 11.1, 17.6, 11.0, 35.0 and 31.2 %, respectively. The same figure representation was used as in Figure 7.

The sensitivities and specificities for these statistics (also see Discussion) are shown in the table.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>CAT</th>
<th>JPSTH</th>
<th>SCCC</th>
<th>FRH</th>
<th>MI</th>
<th>FR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sensitivity (%)</td>
<td>88.7</td>
<td>85.4</td>
<td>82.8</td>
<td>60.2</td>
<td>65.0</td>
<td>51.2</td>
</tr>
<tr>
<td>Specificity (%)</td>
<td>82.4</td>
<td>77.9</td>
<td>77.9</td>
<td>85.3</td>
<td>95.6</td>
<td>100</td>
</tr>
</tbody>
</table>

Figure S4
S5: Movies of CATs in a MEA culture: before and after tetanization.

Different patterns of CATs were obtained from evoked responses to different probe electrodes in MEA cultures. Also, CATs from the same probe electrode were found different before and after tetanization (shown Movie S5a and Movie S5b, respectively). A. The rasterplot of 10 seconds of network activity at 60 electrodes. Evoked responses to different probe electrodes are shown in different colors (the same color was used for the same probe electrode in 2 movies). B. Activity distribution in 60-channel MEA. Activity intensity at different electrodes is shown by black filled circles with different sizes. The locations of probe electrodes are indicated by crosses with the corresponding colors shown in A. C. The corresponding CATs. The color of the trajectory represents the corresponding evoked response shown in A. The scales in the 2 movies are the same. Time is represented in the red bar at the bottom of A.
S6: CATs in all experiments in MEA cultures: before and after tetanization.

Different patterns of CATs were obtained before and after tetanization from 6 experiments in MEAs (see figure). CATs obtained before tetanization (Pre) and after tetanization (Post) for each probe electrode are shown. The column-row numbers of corresponding probe electrodes are shown in the 8 by 8 MEA grids shown in the middle. The tetanization electrodes are depicted by thick black circles. For each probe, CATs calculated for each “block” (see Methods) are shown in black lines and overlaid. The averaged CATs are shown in colored circles (from blue to red).
S7: Calculation of center of weights (CW) for simulations.

Plastic changes in the simulated networks’ functional architecture can be represented by the trajectory of the center of weights (CW). Let $W_i(t)$ be the weight of synapse $i$ at time $t$. Let $X_i$ and $Y_i$ indicate the horizontal and vertical distances from the post-synaptic neuron of the synapse $i$ to a reference point (the center of the dish was used). Then, CW of time $t$ is a two dimensional vector:

$$\vec{CW}(t) = \frac{\sum_{i=1}^{N} W_i(t) \begin{bmatrix} X_i \\ Y_i \end{bmatrix}}{\sum_{i=1}^{N} W_i(t)}$$

where $N$ is the total number of excitatory synapses. Note that while CAT describes the spatiotemporal patterns of signal propagation, CW shows the dynamics of connection strengths.
References


